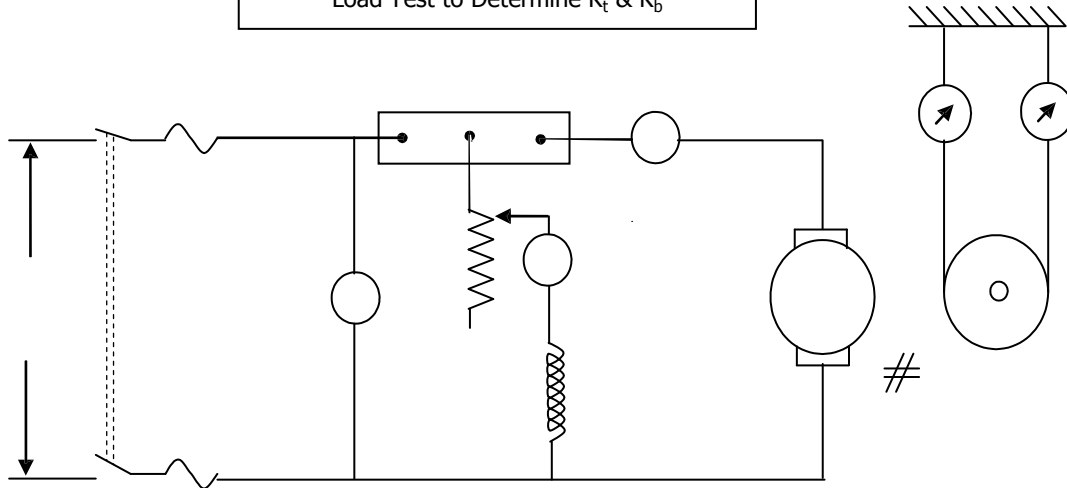


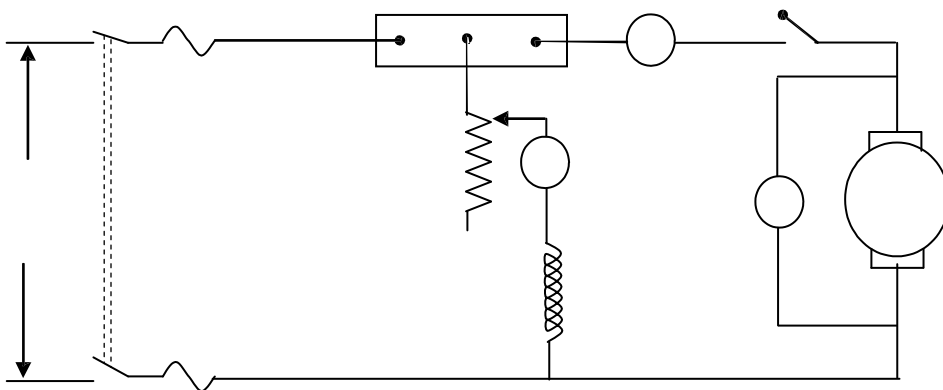






Load Test to Determine  $K_t$  &  $K_b$ 

Retardation Test to Find J &amp; F



**Exp. No.:****Date:****Transfer Function of Armature Controlled DC Motor****Aim:**

To determine the transfer function of an armature controlled dc shunt motor.

**Name Plate Details:**

Power :  
 Voltage :  
 Current :  
 Speed :

**Apparatus Required:**

Sl.No	Name of the Apparatus	Range	Type	Qty
1.	Voltmeter			
2.	Ammeter			
3.	Rheostat			
4.	Tachometer			
5.	Lamp Load			

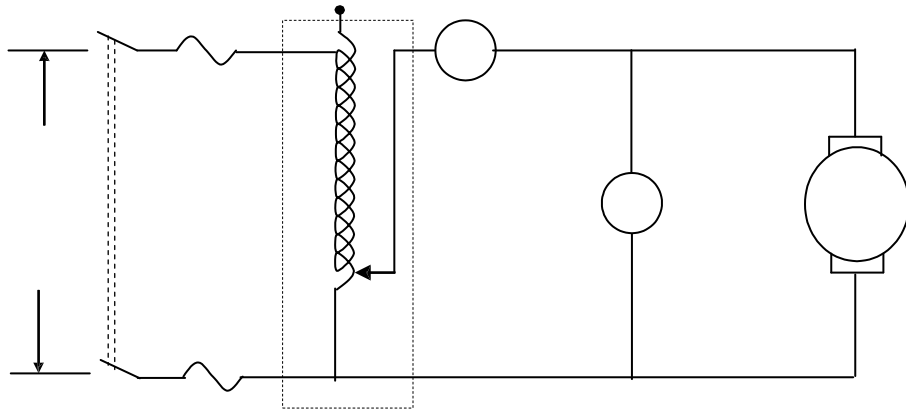
**Theory:**

The transfer function is defined as the ratio of Laplace transformation of the output variable to the Laplace transformer of input variable. The DC motor converts electrical energy into mechanical energy. The electrical energy supplied at the armature terminals converted into controlled mechanical energy.

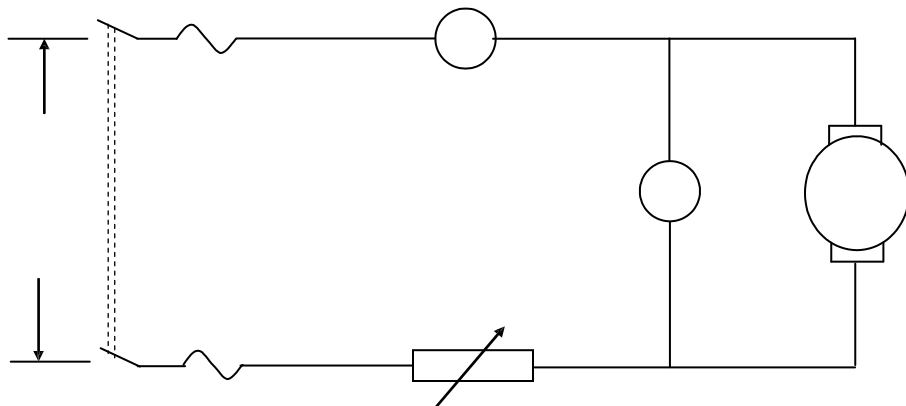
**(i) Armature controlled DC shunt motor**

In armature control, the field current is kept constant and the armature voltage is varied and hence the speed is varied. The field current  $I_f(t)$  is maintained constant by keeping the  $V_f(t)$  to a constant value  $V_f$  and the armature current  $I_a(t)$  is varied to change the torque  $T_m(t)$  of

**To Find  $Z_a$ :-**



**To Find  $R_a$ :-**



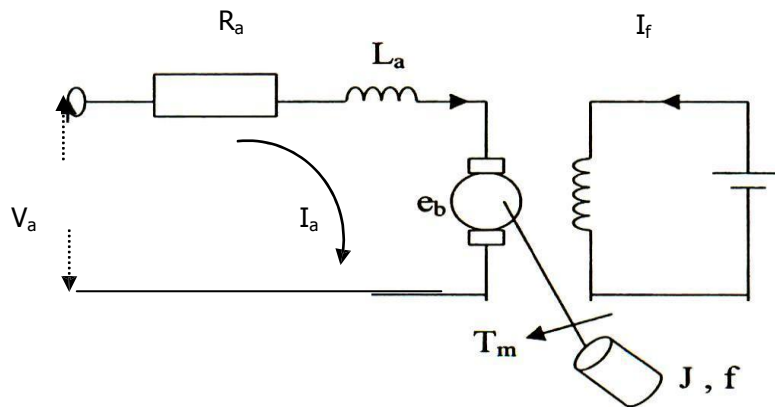
the load connected to the motor shaft. Thus the input variable of the motor is the armature voltage  $V_a(t)$  and the output variable is the torque  $T_m(t)$ . The speed of the DC motor is directly proportional to the armature voltage and inversely proportional to the flux in the armature.

$$\text{i.e. } N \propto V_a / \phi$$

In the armature controlled DC motor, the desired speed is obtained by varying the armature voltage.

Transfer Function by Kirchoff's law,

$$V_a = I_a R_a + L_a \frac{dI_a(t)}{dt} + E_b(t) \dots \dots \dots (1)$$



Taking Laplace transform of equation (1), we have

$$V_a(s) = [R_a + sL_a] I_a(s) + E_b(s)$$

$$\Rightarrow I_a(s) = [V_a(s) - E_b(s)] / [R_a + sL_a] \dots \dots \dots (2)$$

Since the field current is kept constant, the torque developed is proportional to the armature current, i.e., the flux developed  $\phi \propto I_f(t)$ ,  $I_f$  is constant

$$\text{Hence torque developed } T \propto I_a, T \propto I_a \Rightarrow T = K_t I_a \dots \dots \dots (3)$$

$$\text{Taking Laplace transform of equation (3), } T(s) = K_t I_a(s) \dots \dots \dots (4)$$

$$\text{Where } K = \text{Torque constant, } K_t = \Delta T / \Delta I_a \text{ N-m / A} \dots \dots \dots (5)$$

**Tabulations:-**To Find  $K_t$  &  $K_b$ :-

$I_f$	$I_a$	$V_a$	N (rpm)	$\omega = 2\pi N/60$ (Rad/sec)	$E_b = V_a - I_a R_a$	$T = E_b I_a / \omega$ (N-m)
Rated Value (0.5A)						

To Find J &amp; F:-

Retardation Test For	Range of Speed (Rpm)	Time (Sec)
J only	1500 to 225	
Both J & F	1500 to 225	

To Find  $R_a$ :-

$v_a$ (V)	$I_a$ (A)	$R_a = V_f / I_f$



The torque equation is given by,

$$T(t) = J_d^2 \theta / dt^2 + f d\theta / dt \dots\dots\dots(6)$$

Taking Laplace transform of equation (6),

$$T(s) = Js^2 \theta(s) + f s\theta(s) \dots\dots\dots(7)$$

Substituting equation (4) in (7),

$$\begin{aligned} K_t I_a(s) &= Js^2 \theta(s) + f s\theta(s) \\ s\theta(s) [Js+f] &= K_t I_a(s) \dots\dots\dots(8) \end{aligned}$$

Substituting equation (2) in (8),

$$s\theta(s) [Js+f] = K_t [V_a(s) - E_b(s)] / [R_a + sL_a] \dots\dots\dots(9)$$

Motor back emf is proportional to speed, i.e.,

$$E_b(t) = K_b d\theta / dt = K_b \omega(t) \dots\dots\dots(10)$$

Where  $K_b$  = back emf constant.

Taking laplace transform of equation (10),

$$E_b(s) = K_b \omega(s) \dots\dots\dots(11)$$

Substituting equation (11) in (9),

$$s\theta(s) [Js+f] = K_t [V_a(s) - K_b \omega(s)] / [R_a + sL_a]$$

$$\omega(s) [Js+f] = K_t [V_a(s) - K_b \omega(s)] / [R_a + sL_a], \text{ since } d\theta / dt = \omega(s) \text{ \& } s\theta(s) = \omega(s)$$

$$\omega(s) / V_a(s) = K_t / K_t K_b + (sJ+f) (R_a + sL_a)$$

Where,  $R_a$  = Armature resistance;  $\Omega$

$L_a$  = Armature Inductance; Hendry

$K_t$  = Torque constant =  $\Delta T / \Delta I_a$ ; N-m / A

$K_b$  = Back emf constant =  $\sim E_b / \sim N$  ; Volts/(rad/sec)

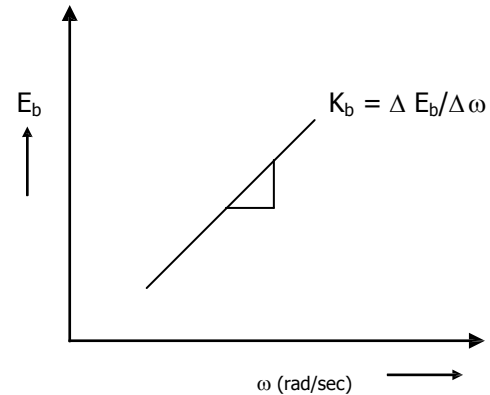
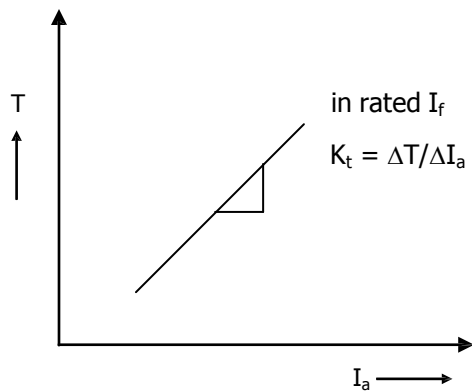
$f$  = Frictional constant; N-m/(rad/sec)

$J$  = moment of Inertia;  $kg \cdot m^2$

To Find  $Z_a$ :-

$V_a$ (V)	$I_a$ (A)	$Z_a = V_f/I_f$

Model Graph: [to find  $K_t$  &  $K_b$ ]



Formulae:

$$\text{Total losses in a circuit} = V (I_a + I_f) - I_a^2 R - V I_f$$

$$\text{Energy} = (\text{Losses} * t) = \frac{1}{2} J (\omega_1^2 - \omega_2^2)$$

$$N_1 = 1500 \text{ rpm}; N_2 = 225 \text{ rpm}; \omega = 2\pi N / 60$$

$$J = (\text{Losses} * t * 2) / (\omega_1^2 - \omega_2^2)$$

$$f = J / \lambda m$$

$$L_a = \sqrt{Z_a^2 - R_a^2} / 2\pi f$$

$f$  = frequency

$$\omega(s) / V_a(s) = K_t / K_t K_b + (sL + f) (R_a + sL_a)$$

**Procedure:****(i) Load test to determine  $K_t$  &  $K_f$** 

- Conduct the load test with normal rated value of field currents.
- Give the connections as per circuit diagram.
- Keep the field rheostat in minimum position & switch on 230 V supply.
- Adjust the field rheostat to rated speed & consider the corresponding field current as rated field current.
- For different loads note down  $I_a, V_a$  & speed
- Calculate the torque developed.
- Plot a graph between T(Y -axis) and  $I_a$  (X-axis) for both the cases.
- From this graph, obtain  $K_t$ .
- Plot the graph between  $E_b$  Vs  $\omega$ .
- From this graph, obtain  $K_b$ .

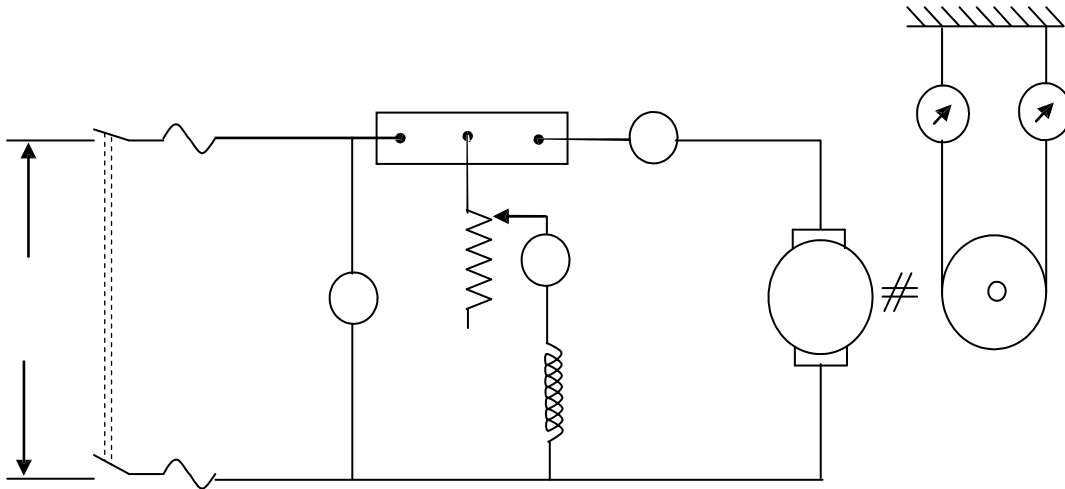
**(ii) Retardation Test to find J & f**

The total losses can be divided into two parts, viz., constant losses and variable losses. The constant losses include frictional & inertia losses.

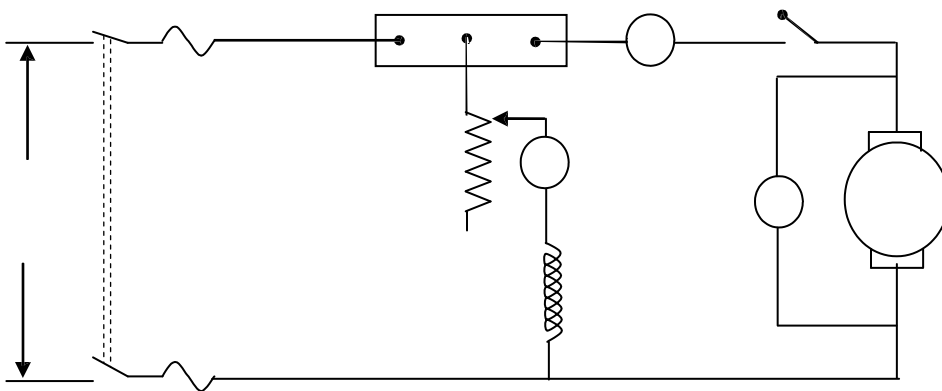
- Give the connections as per circuit diagram.
- By closing the switch, make the measurement of  $V, I_a$  and  $I_f$ .
- Make the motor to run at a speed greater than 1600 RPM.
- Open the switch suddenly.
- Using stopwatch, note down the time taken for the speed of the motor to fall down from ( $\omega_1 = 1500$  rpm,  $\omega_2 = 225$  rpm)
- The moment of inertia, J is obtained from the relation between loss, time and  $\omega$
- The friction constant, f is obtained using the exponential relation between speed, time and time constant.  $\zeta m = t_1 \sim t_2 / \ln(N_1 - \ln N_2)$   $\curvearrowright$  natural log
- Calculate no load input power using the values read by ammeter & voltmeter connected to armature circuitry.

**Result:**

Thus the transfer function of dc shunt motor by armature control is determined.

Load Test to Determine  $K_t$  &  $K_b$ 

Retardation Test to Find J &amp; F



**Exp. No.:****Date:****Transfer Function of Field Controlled DC Motor****Aim:**

To determine the transfer function of a field controlled dc shunt motor.

**Name Plate Details:**

Power :  
 Voltage :  
 Current :  
 Speed :

**Apparatus Required:**

Sl.No	Name of the Apparatus	Range	Type	Qty
1.	Voltmeter			
2.	Ammeter			
3.	Rheostat			
4.	Tachometer			
5.	Lamp Load			

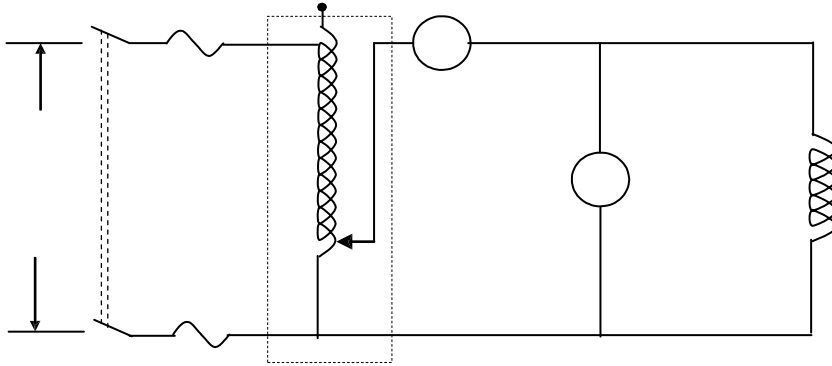
**Theory:**

The transfer function is defined as the ratio of Laplace transform of the output variable to the Laplace transform of input variable. The DC motor converts electrical energy into mechanical energy. The electrical energy supplied at the armature terminals converted into controlled mechanical energy.

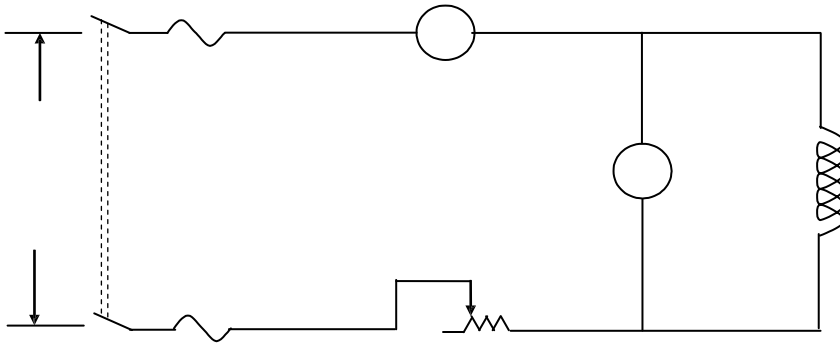
**(ii) Field Controlled DC Shunt Motor**

In field control method, the armature current  $I_a(t)$  is maintained to a constant value  $I_a$  while the field voltage  $V_f(t)$  is varied to control the speed or torque of the motor. Thus the input of the motor is field voltage  $V_f(t)$  and the output is the motor speed and the load displacement.

**To Find  $Z_f$  :-**

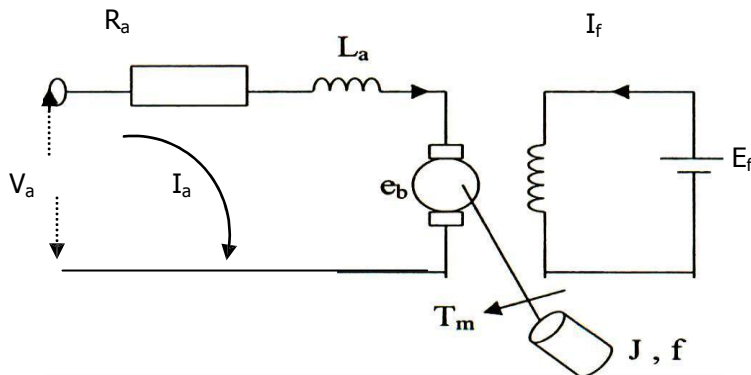


**To Find  $R_f$  :-**



**Transfer Function:**

The circuit for field controlled dc shunt motor is given in figure.



Where,  $R_f$  = Resistance of field circuit ; $\Omega$   
 $L_f$  = Inductance of field circuit; Henry  
 $E_f$  = Excitation voltage; Volts  
 $I_f$  = Excitation current; Amperes  
 $J$  = Moment of Inertia;  $\text{kg}\cdot\text{m}^2$

$f$  = Co efficient of friction ; $\text{N}\cdot\text{m} / (\text{rad}/\text{sec})$

$\omega$  = Angular velocity =  $d\theta/dt$  in  $\text{rad}/\text{sec}$

Applying Kirchoffs law,

$$E_f(t) = R_f I_f(t) + L_f dI_f(t)/dt \dots\dots\dots(1)$$

Taking Laplace transform of equation (1)

$$E_f(s) = R_f I_f(s) + L_f s I_f(s), \text{ which implies } I_f(s) = E_f(s) / [R_f + sL_f] \dots\dots\dots(2)$$

The torque developed is proportional to the field current, since the armature current is constant i.e.

$\phi \propto I_f$  &  $T \propto \phi I_a$  as  $I_a$  is constant,  $T \propto \phi$ , which implies  $T \propto I_f$

$$T = K_f I_f(t) \dots\dots\dots(3)$$

Where  $K_f = \Delta T / \Delta I_f = \text{Constant}$  in  $\text{N}\cdot\text{m} / \text{amperes} \dots\dots\dots(4)$

$$\text{Taking laplace transform of equation (3), } T(s) = K_f I_f(s) \dots\dots\dots(5)$$

The torque equation is given by,

$$T(t) = J d^2\theta/dt^2 + f d\theta/dt = J d\omega/dt + f\omega$$

Taking laplace of the above equation,

$$T(s) = Js\omega(s) + f\omega(s) \dots\dots\dots(6)$$

Substituting equation (5) in (6),

$$K_f I_f(s) = Js\omega(s) + f\omega(s), \text{ which implies } \omega(s) = K_f I_f(s) / [Js + f] \dots\dots\dots(7)$$

Substituting equation (2) in (7),

$$\omega(s) / E_f(s) = K_f / \{ [sJ + f] [R_f + sL_f] \}$$

**Tabulations:-**To Find  $K_f$ :-

$I_f$	$I_a$	$V_a$	N (rpm)	$\omega = 2\pi N/60$ (Rad/sec)	$E_b = V_a - I_a R_a$	$T = E_b I_a / \omega$ (N-m)
Rated Value (0.5A)						
80 % Rated Value						

To Find J &amp; F:-

Retardation Test For	Range of Speed (Rpm)	Time (Sec)
J only	1500 to 225	
Both J & F	1500 to 225	



**Procedure:****(i) Load test to determine  $K_f$** 

- Conduct the load test with two constants normal (rated value) & sub normal (say 80% of rated field current) values of field currents.
- Give the connections as per circuit diagram.
- Keep the field rheostat in minimum position & switch on 230 V supply.
- Adjust the field rheostat to rated speed & consider the corresponding field current as rated field current.
- For different loads note down  $I_a, V_a$  & speed
- Calculate the torque developed.
- Repeat the same for 80% of excitation current.
- Plot a graph between T (Y-axis) and  $I_a$  (X-axis) for both the cases.
- From the graph deduce two points ( $T_1, I_{f1}$  and ( $T_2, I_{f2}$ ) for the same armature current ( $I_a =$  rated or maximum value).
- Plot the graph between T Vs  $I_f$
- From this graph, obtain  $K_f$ .

**(ii) Retardation Test to find J & f**

The total losses can be divided into two parts, viz., constant losses and variable losses. The constant losses include frictional & inertia losses.

- Give the connections as per circuit diagram.
- By closing the switch, make the measurement of  $V, I_a$  and  $I_f$ .
- Make the motor to run at a speed greater than 1600 RPM.
- Open the switch suddenly.
- Using stopwatch, note down the time taken for the speed of the motor to fall down from ( $\omega_1 = 1500$  rpm,  $\omega_2 = 225$  rpm)
- The moment of inertia, J is obtained from the relation between loss, time and  $\omega$
- The friction constant, f is obtained using the exponential relation between speed, time and time constant.  $\zeta m = t_1 \sim t_2 / \ln(N_1 - \ln N_2)$
- Calculate no load input power using the values read by ammeter & voltmeter connected to armature circuitry.

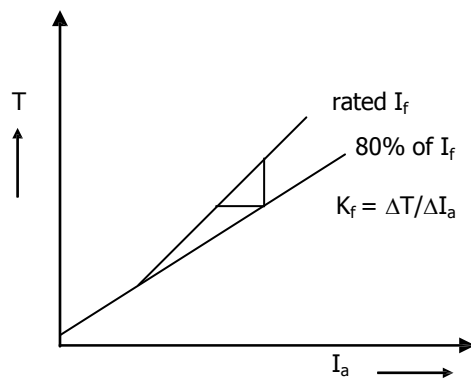
To Find  $R_f$ :-

$V_f$ (V)	$I_f$ (A)	$R_f = V_f/I_f$

To Find  $Z_f$ :-

$V_f$ (V)	$I_f$ (mA)	$Z_f = V_f/I_f$ (K $\Omega$ )

Model Graph: [to find  $K_t$  &  $K_b$ ]



**Formulae:**

$$\text{Total losses in a circuit} = V (I_a + I_f) - I_a^2 R - V I_f$$

$$\text{Energy} = (\text{Losses} * t) = \frac{1}{2} J (\omega_1^2 - \omega_2^2)$$

$$N_1 = 1500 \text{ rpm}; N_2 = 225 \text{ rpm}; \omega = 2\pi N/60$$

$$J = (\text{Losses} * t * 2) / (\omega_1^2 - \omega_2^2)$$

$$f = J / \zeta m$$

$$L_f = \sqrt{Z_f^2 - R_f^2} / 2\pi f$$

$$\omega(s) / E_f(s) = K_f / \{ [sJ + f] [R_f + sL_f] \}$$

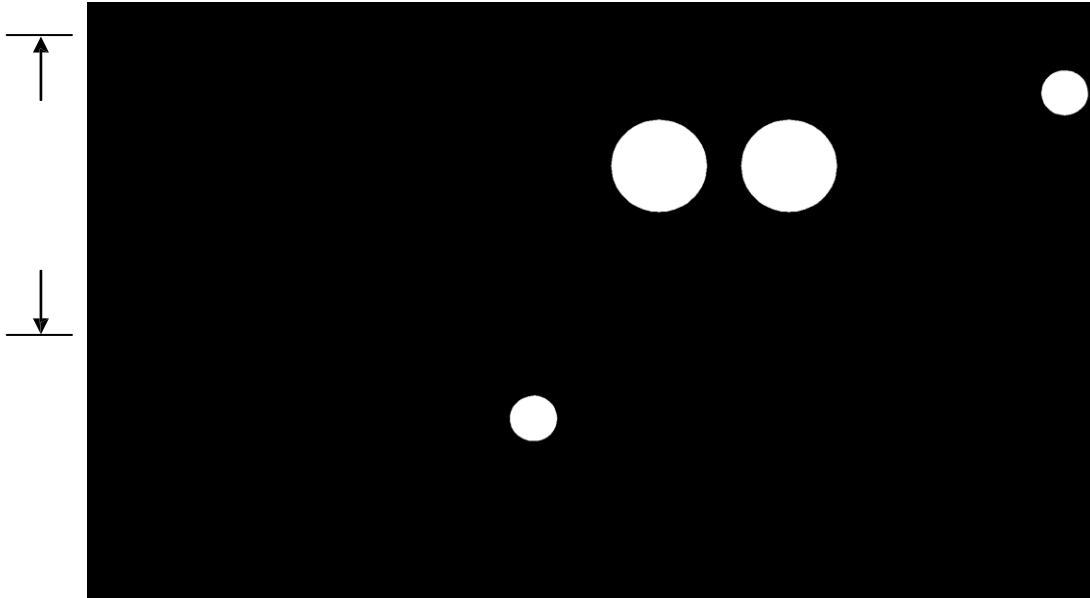
**(iii) V-A method to obtain  $L_f$** 

- Give the connections as per circuit diagram.
- Measure  $R_a$  &  $R_f$ . [As the field winding resistance is of the order of 250-3000hms and it can withstand a current of 1A, the circuit shown can be used for measurement of  $R_f$ . Similarly, as the armature resistance is of order of 0.2 - 1 ohms and it can be measured using the circuit shown]
- To measure  $L_f$  &  $L_a$ , give the connections as shown.
- Apply an ac voltage & measure the field reactance  $Z_r$  & armature reactance  $Z_a$ .
- Calculate  $X_f = \text{Square root of } Z_f^2 - R_f^2$  and  $L_f = \text{Square root of } (Z_f^2 - R_f^2) / 2\pi f$

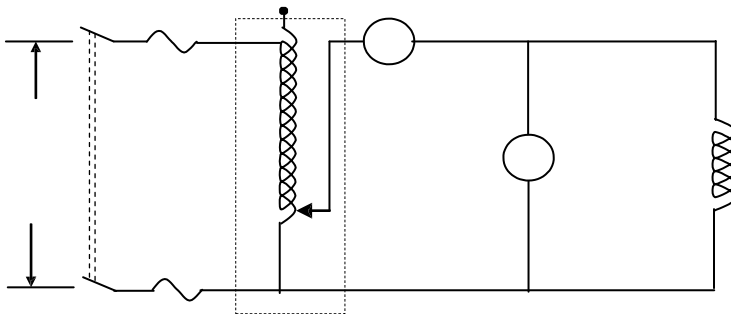
**RESULT:**

Thus the transfer function of dc shunt motor by field-control method is determined.

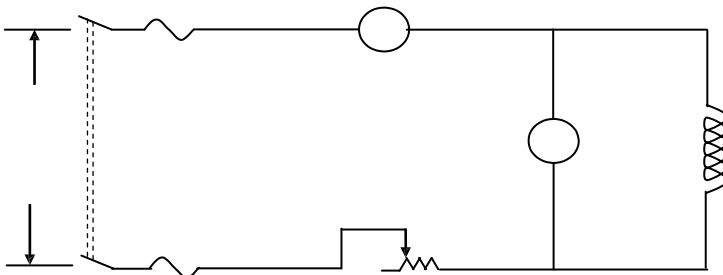
## Transfer function of separately excited dc shunt generator on load



To Find  $Z_f$  :-



To Find  $R_f$  :-



**Exp.No.:****Date:****Transfer function of separately excited dc shunt generator on load****Aim:-**

To determine the transfer function of Separately Excited DC generator on load condition.

**Name Plate Details:**

Power :  
 Voltage :  
 Current :  
 Speed :

**Apparatus Required:**

Sl.No	Name of the Apparatus	Range	Type	Qty
1.	Voltmeter			
2.	Ammeter			
3.	Rheostat			
4.	Tachometer			
5.	Lamp Load			

**Precautions:-**

1. Field rheostat at motor side should be at minimum resistance position.
2. Potential divider must be kept at minimum potential position.
3. Starter handle should be at OFF position.
4. DPST switch should be in open.

**Procedure:-**

1. Connections are made as per the circuit diagram.
2. Close the DPST switch.
3. Start the motor with the help of 3 point starter.
4. By adjusting the field rheostat in the motor side the machine is made to run in the rated speed of the generator.

**Tabulations:-**To find  $R_L$ :-

S.No	Generated voltage ( $I_g$ )	Generated current $I_g$	$R_L = E_g/I_g$

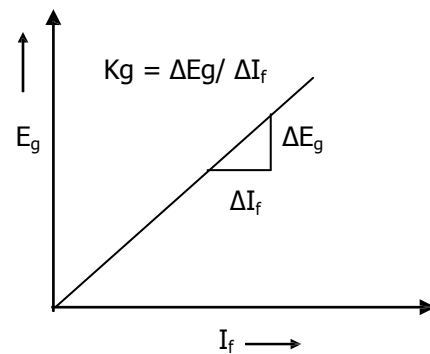
To find  $Z_f$ :-

S.No	$V_f$	$I_f$	$Z_f = V_f/I_f$	$X_f = \sqrt{(Z_f^2 - R_f^2)}$	$L_f = X_f/2\pi f$

To find  $R_f$ :-

S.No	$V_f$	$I_f$	$R_f = V_f / I_f$

Model graph:



5. Note the value of field current, field voltage generated voltage when the field current is zero.
6. By varying the potential divider find out  $I_f$ ,  $E_g$ ,  $V_g$ , which are used to calculate  $R_L$ ,  $R_f$ .
7. To find the  $R_{eff}$ , find the armature resistance of the generator.
8. Auto transformer is used to find field impedance, field reactance and field inductance.

### Formulae:

$$\text{Transfer function: } \frac{E_o(s)}{E_f(s)} = \frac{K}{1+sT}$$

Where,

$$K = K_g/R_f \text{ (no unit)}$$

$$K_g = \text{Generated emf constant}$$

$$R_f = \text{Field resistance}$$

$$K_g = \Delta E_g / \Delta I_f$$

Where,

$$\Delta E_g = \text{Voltage generated}$$

$$\Delta I_f = \text{Field Current}$$

$$T = L_f/R_f$$

Where,

$$T = \text{Time constant}$$

$$L_f = \text{Field Inductance}$$

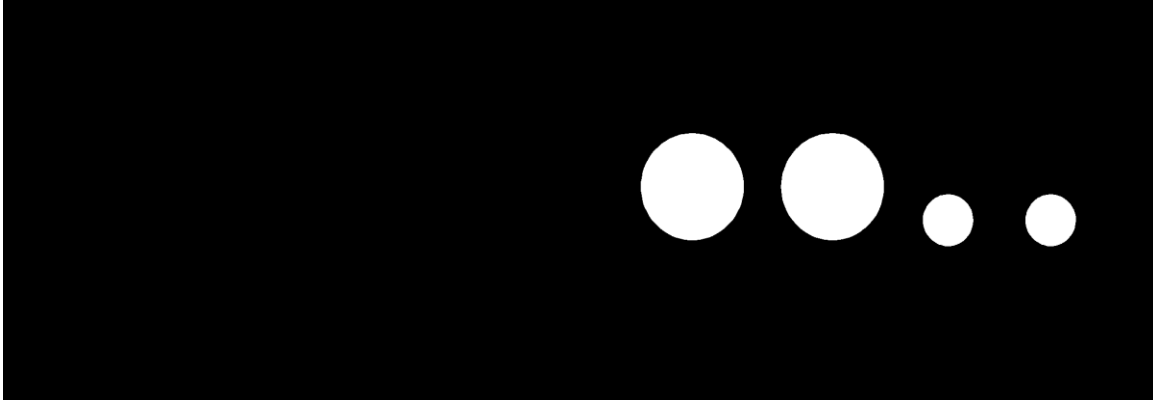
$$R_f = \text{Field Resistance}$$

### Result:-

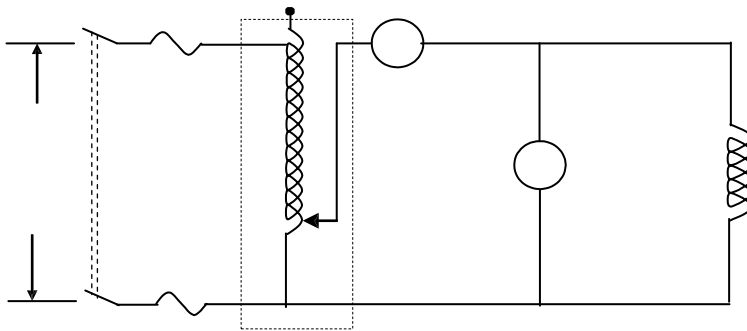
Thus the transfer function of Separately Excited DC generator on load condition is successfully determined.

The transfer function is 
$$\frac{E_o(s)}{E_i(s)} =$$

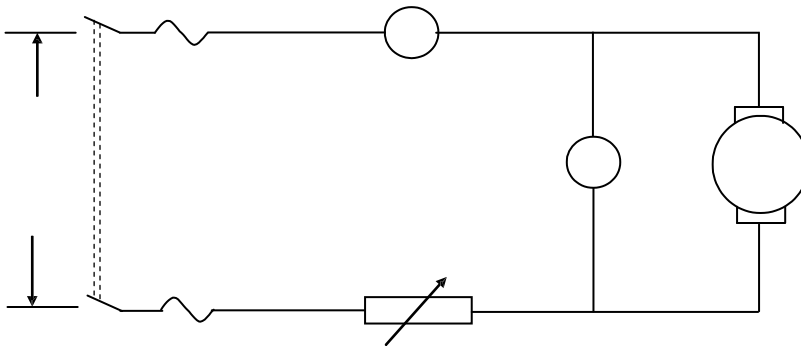
Transfer function of self excited DC shunt generator on load condition



**To Find  $L_f$  :-**



**To Find  $R_a$  :-**





**Exp.No.:****Date:****Transfer function of self excited DC shunt generator on load condition****Aim:-**

To determine the transfer function of self excited DC shunt generator on load condition.

**Name Plate Details:**

Power :  
 Voltage :  
 Current :  
 Speed :

**Apparatus Required:**

Sl.No	Name of the Apparatus	Range	Type	Qty
1.	Voltmeter			
2.	Ammeter			
3.	Rheostat			
4.	Tachometer			
5.	Lamp Load			

**Precautions:-**

1. Field rheostat of motor should be kept at minimum resistance position.
2. Potential divider must be kept at minimum potential position.
3. Starter handle should be at OFF position.
4. DPST switch should be kept at OFF before starting the motor.

**Procedure:-**

1. Connections are made as per the circuit diagram.
2. Close the DPST and start the motor with the help of the three point starter.
3. By adjusting the field rheostat on the motor side the machine is made to run at rated speed.

**Tabulations:-**To find  $K_g$  &  $R_f$ .

S.No	$V_f$ (volts)	$I_f$ (A)	$I_L$ (A)	$E_g$ (V)	$R_f = V_f/I_f$	$R_L = E_g/I_L$

To find  $R_a$ 

S.No	$V_a$ (volts)	$I_a$ (amp)	$R_a = V_a/I_a$

To find  $L_f$ :-

S.No	$V_f$ (volts)	$I_f$ (mA)	$Z_f = V_f/I_f$	$X_f = \sqrt{Z_f^2 - R_f^2}$	$L_f = X_f/2\pi f$

4. Note down the value of field current and voltage generated voltage the field current at zero.
5. By varying the loading rheostat the corresponding values of ammeter and voltmeter readings are noted.

**Formula :-**

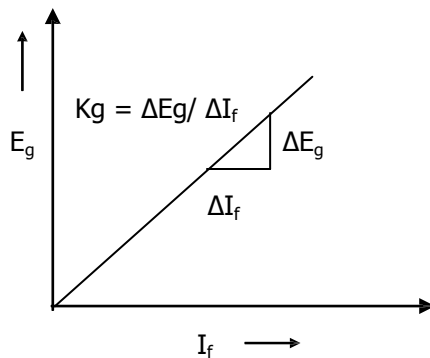
$$\text{Transfer function } T(s) = \frac{K}{1+sT}$$

$$\text{Where, } K = \frac{K_g R_L}{R_f (R_a + R_L)}$$

$$K_g = \Delta E_g / \Delta I_f$$

$$T = L_f / R_f$$

**Model graph:**

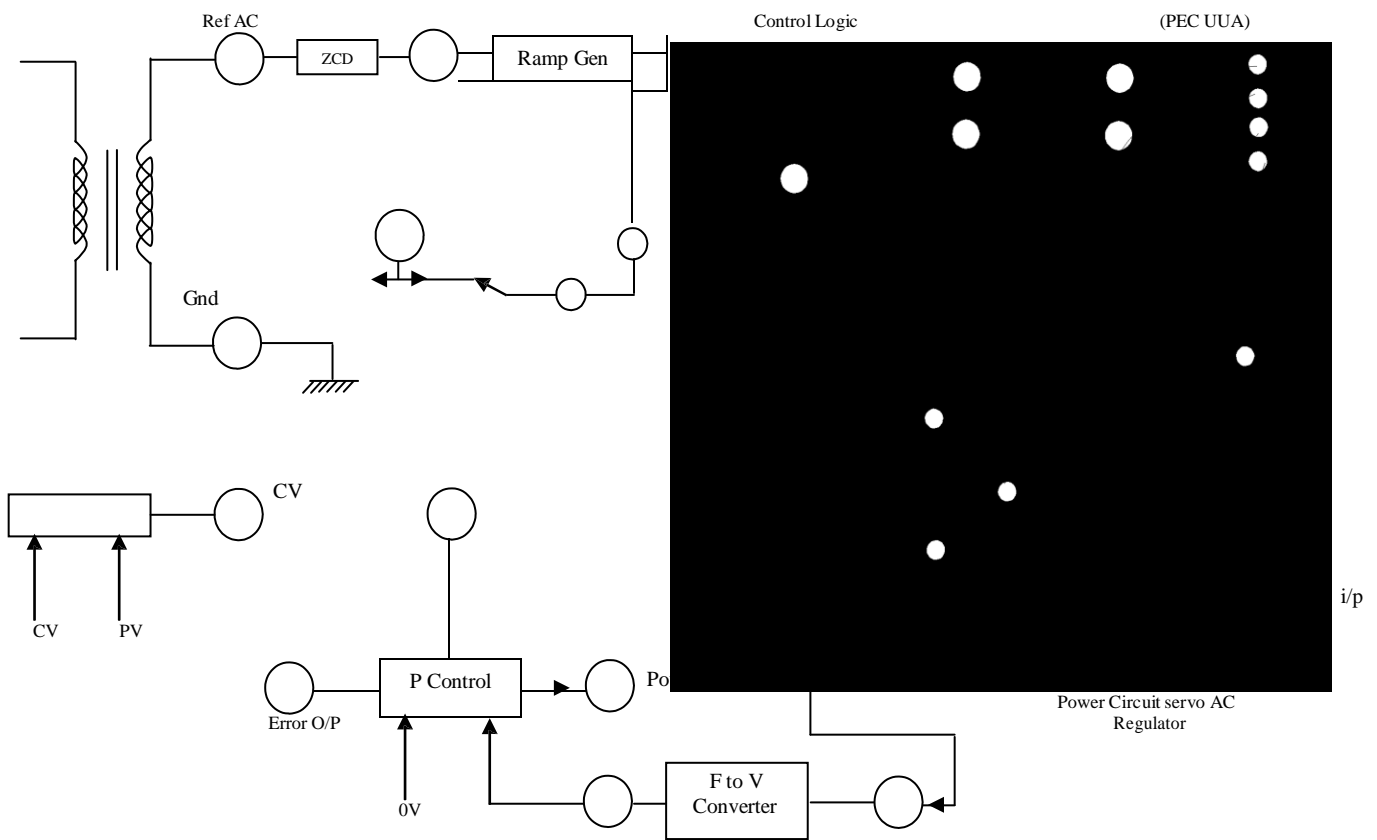


**Result:-**

Thus the transfer function of self excited DC shunt generator on load condition is determined and is found to be,

$$T(s) = K / (1+sT)$$

Measurement of Transfer Function Parameters of AC servomotor



**Exp.No:****Date:****Measurement of Transfer Function Parameters of AC servomotor****Aim:**

To determine the motor constants  $K_u$  and  $K_z$  and to find transfer function of motor.

**Apparatus Required:**

1. Voltmeter ( 0- 20 ) V Mc
2. Patch chards
3. Single phase AC servomotor speed control and transfer function study trainer kit.

**Procedure:****To determine value of  $k_z$  :-**

1. Connect  $G_1K_1$  of pulse isolation output to  $G_1K_1$  of SCR.
2. Connect  $G_2K_2$  of pulse isolation output to  $G_2K_2$  of SCR
3. To operate open loop control mode using switch  $S_1$ .
4. 9 – pin - D connector is connected from over setup to back side of trainer.
5. Keep speed indicator switch in PV mode.
6. Connect AC voltmeter ( 0 – 20 )V or Multimeter across the control phase winding  $C_1$  and  $C_2$ .

**Experimental Procedure:-**

1. Switch on 230V AC supply to winding reluctance.
2. Switch on 230V AC supply to motor setup.
3. Switch on pulse on/off switch  $S_2$ .
4. Vary control voltage pot and set the rated voltage ( 11.4 ) to control phase winding.
5. Apply load on motor step by step to motor upto zero rpm.
6. For each step, note readings ( load, speed ) as shown.
7. Calculate torque value.
8. Plot graph speed vs torque.
9. Slope of speed torque curve gives  $K_2$ .

**To determine the value of  $K_1$** 

1. Connects  $G_1K_1$  of pulse isolation output to  $G_1K_1$  of SCR<sub>1</sub>.
2. Connects  $G_1K_1$  of pulse isolation output to  $G_2K_2$  of SCR<sub>2</sub>.
3. To operate open loop control mode using switch  $S_1$ .

**TABULATION:-**

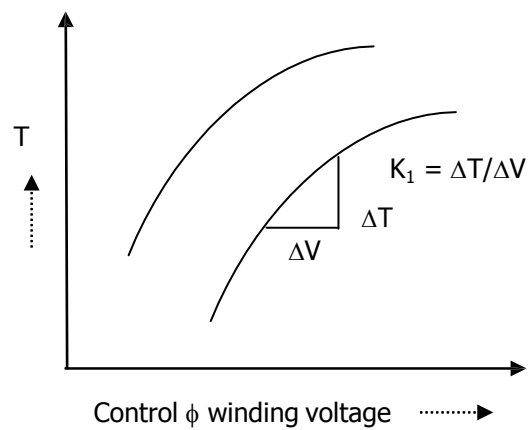
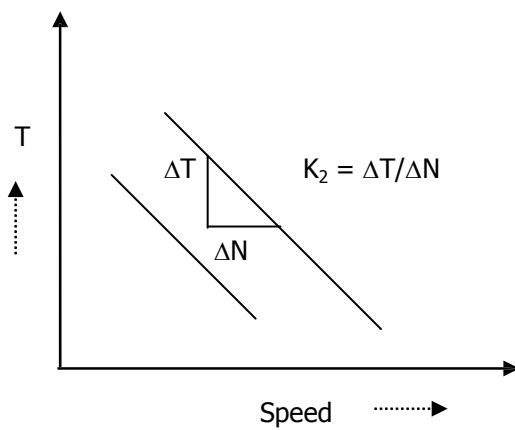
Control voltage = Rated voltage.

For  $K_2$ :-

Speed (rpm)	Load ( $K_g$ )	Torque (nm)

For  $K_1$ :-

Load ( $K_g$ )	Control Voltage (V)	Torque (nm)

**Model Graph:-**

4. 9 pin D connector is connected from motor setup to back side of trainer.
5. Keep speed indicator switch in PV mode.
6. Connects AC Voltmeter ( 0-20)V of Multimeter across control phase winding.

#### Experimental procedure:-

1. Switch ON the 230V AC supply to reference winding.
2. Switch ON the 230V AC supply to motor setup.
3. Switch ON the pulse ON/OFF switch  $S_2$ .
4. Vary control voltage pot or and set the rated voltage to control phase winding.
5. Apply load on motor, step by step up to zero rpm.
6. For each step, note down load and voltmeter readings.
7. Calculate torque and the plot graph torque vs control voltage.
8. A slope of torque vs control voltage curve gives motor constant  $K_2$ .

#### From observation:-

$$K_2 = 2 \times 10^{-5}; \quad K_1 = 7.5 \times 10^{-3}$$

$$T.F = \frac{W(S)}{E_c(S)} = \frac{K_1}{SJ + K_2 + B} = \frac{K_m}{1 + ST_m}$$

$$K_m = K_1 / K_2 + B \Rightarrow \text{Motor gain Constant}$$

$$T_m = J / K_2 + B \Rightarrow \text{Motor time Constant}$$

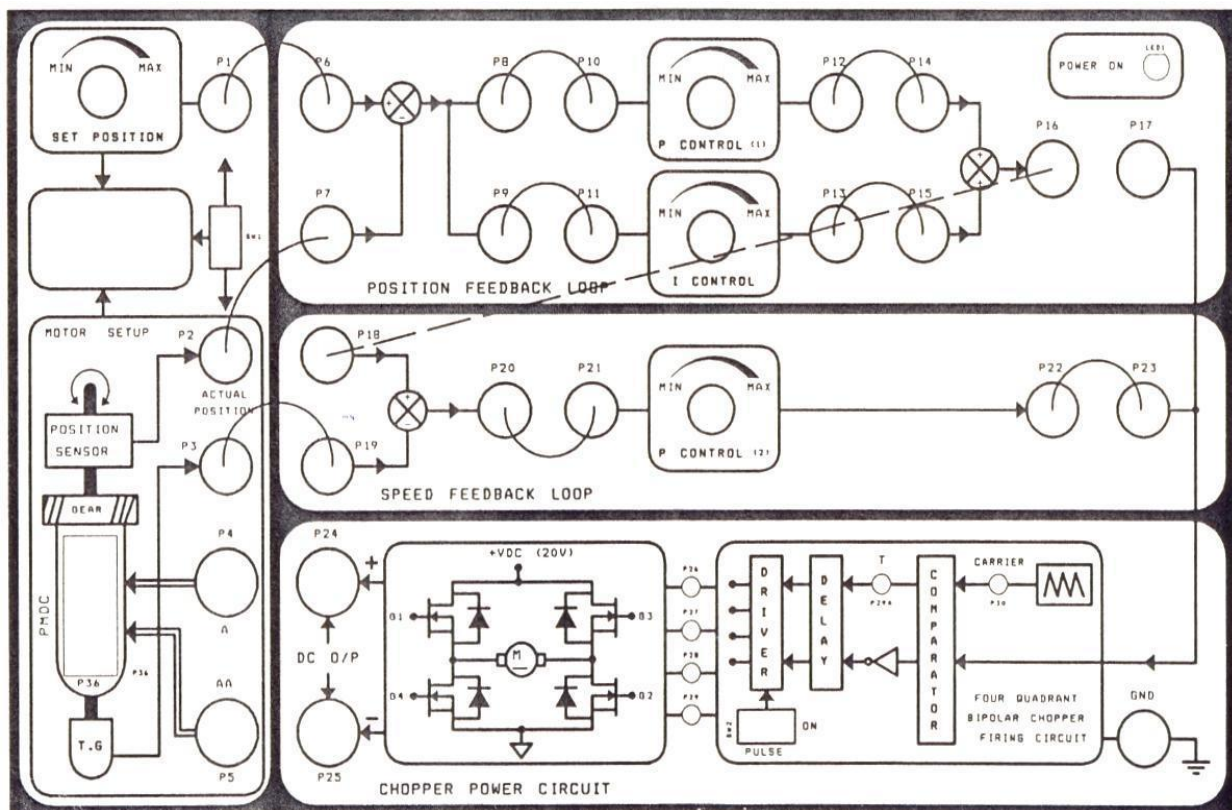
$$J = 52 \text{ gm/cm}^2 \quad B = 0.01875$$

#### Result:-

Thus motor constants  $K_1$  and  $K_2$  are obtained and AC servo motor T.F is:-

$$\frac{W(s)}{E(s)} = \frac{K_1}{SJ + K_2 + B} = \frac{K_m}{1 + ST_M} =$$

Dc Servomotor Position Controller





**Exp. No:**

**Date:**

### **DC Servomotor Position Controller**

**Aim:-**

To study the DC servomotor position controller with PI control.

**Apparatus Required:-**

1. PEC – 01
2. Connecting Wires
3. Motor setup

**Procedure:-**

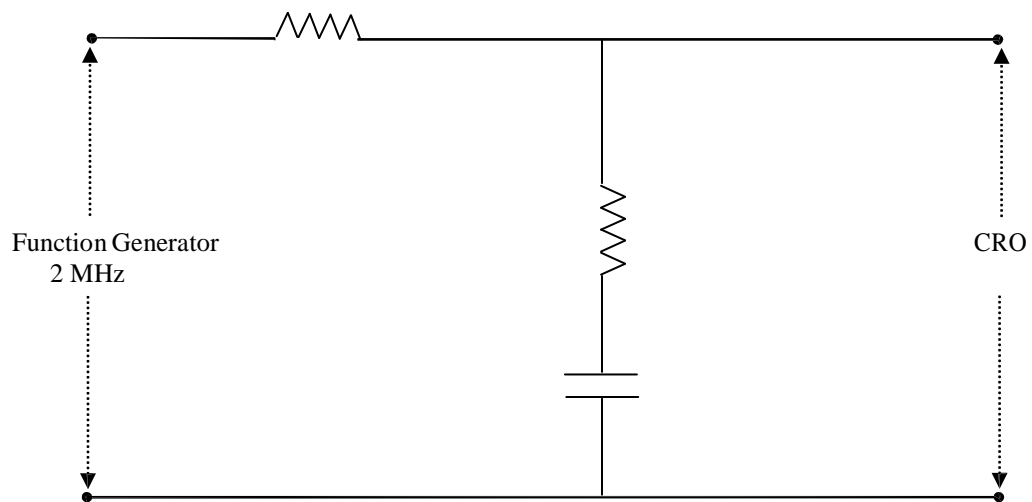
1. Connections are given as per circuit diagram.
2. Checks whether the pulse release switch is in OFF position.
3. If it is in ON position by varying the set position.
4. Switch on the unit.
5. Set the motor at any position by varying the set position.
6. Notice the input position in digital display.
7. Now release the pulse and release the switch also, so at the same time there is no voltage.
8. Note output position in digital display.
9. Tabulate the input and output position voltage at  $S_p$  and  $P_r$ .

**Tabulation:-**

Set Point (Sp)		Motor Position Variables (Pr)				Error	
Q (deg)	V (volts)	Before		After		Before (v)	After (v)
		Q (deg)	V (volts)	Q (deg)	V (volts)		

**Result:-**

DC Servomotor position controller was studied with PI controller.

**LAG NETWORK**

**Exp. No:****Date:****STUDY OF LAG NETWORK****Aim:-**

To obtain the transfer function and hence identify the components of LAG network.

**Apparatus Required:-**

Sl.No	Name of the apparatus	Range	Type	Qty

**Procedure:-**

1. The resistor values are chosen and the connections are made as per the circuit diagram.
2. The input voltage of required volt is given from function generator.
3. The frequency range is chosen for the corresponding frequency of the out put  $v_o$ , a and b component are noted.
4. For various frequency this steps are repeated.
5. The gain is  $20 \log v_o/v_{in}$  in db.

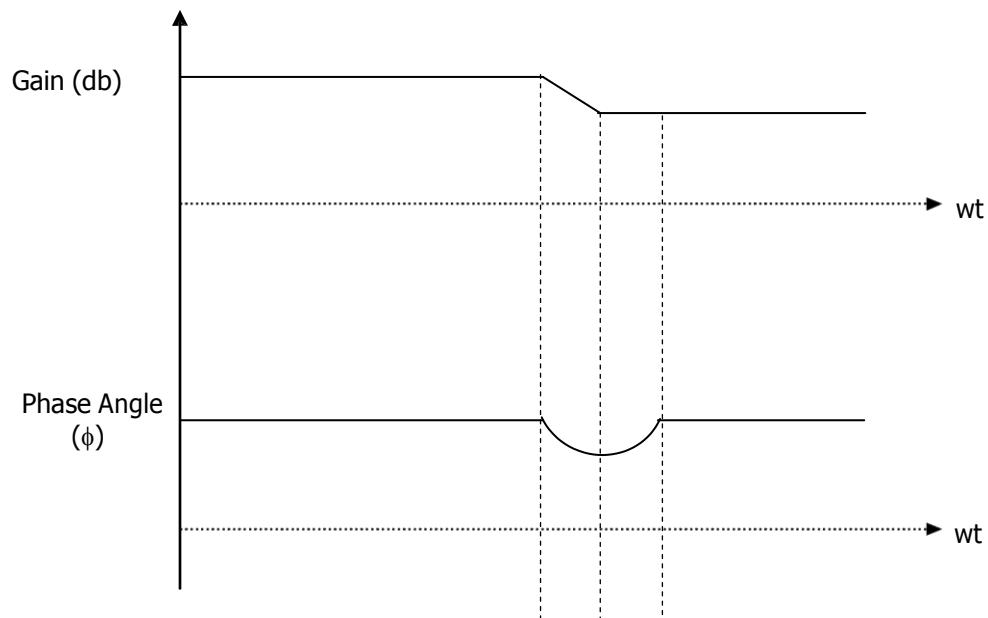
**Theory:-**

This consists of inserting an extra pole into the transfer function at a lesser frequency than the existing poles. This introduces a phase lag into the amplifier. Hence the loop gain becomes 0 db with a slope of 6 db per of frequency where the poles of  $A_v$  contribute negligible phase shift.

The additional of dominant frequency may be easily realised by adding simple Rc network.

**Tabulation :-**

Sl.No.	Frequency	Out put voltage (v)	Gain $A_v = 20 \log v_o/v_{in}$	Phase angle ( $\phi$ )

**Model Graph:-**

**Formula :-**

$$\phi = \tan^{-1} (R_2 / \omega c) - \tan^{-1} (R_1 + R_2) / \omega c$$

$$\text{Gain: } A = 20 \log (v_o / v_{in}) \text{ db}$$

$$\text{Transfer function: } \frac{R_2 + sR_1 R_2 c}{(R_1 + R_2) s R_1 R_2 c}$$

**Design theory:-**

$$\begin{aligned} E_i(t) &= (z_1 + z_2) i(t) \\ &= (R_1 + R_2) i(t) + 1/C \int i(t) dt \end{aligned}$$

$$E_o(t) = z_2 \int i(t) dt$$

$$E_o(t) = R_2 i(t) + 1/c \int i(t) dt$$

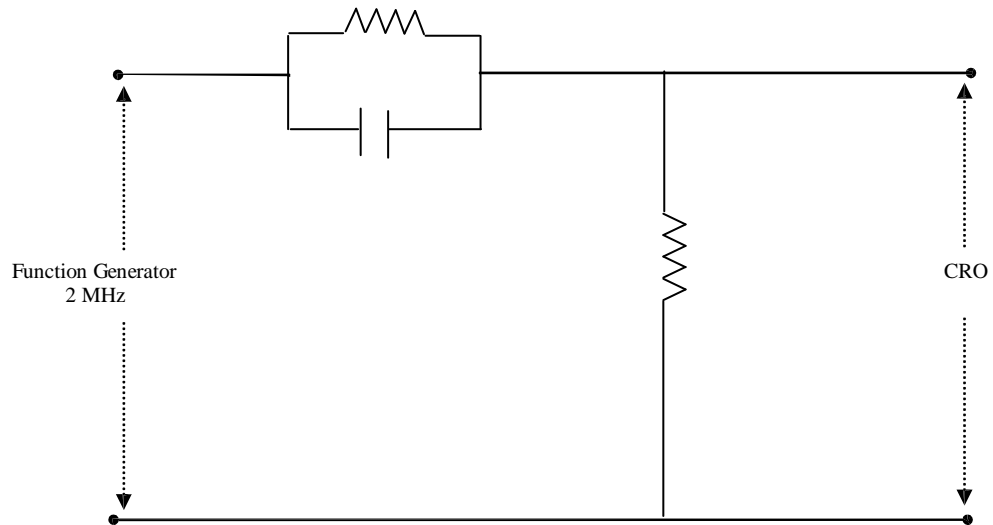
Taking laplace transform (1) & (2) we get

$$E_i(s) = (R_1 + R_2) I(s) + 1/CS I(s)$$

$$E_o(s) = R_2 I(s) + 1/CS I(s)$$

**Result:-**

Thus the lag compensator was analyzed and transfer function of lag compensator was determined.

**LEAD NETWORK**



**Exp. No:****Date:****STUDY OF LEAD NETWORK****Aim:-**

To obtain the transfer function and hence identify the components of a lead network.

**Apparatus Required:-**

Sl.No	Name of the apparatus	Range	Type	Qty

**Procedure:-**

1. The resistor values are chosen and the connections are made as per the circuit diagram.
2. The input voltage of required volt is given from function generator.
3. The frequency range is chosen for the corresponding frequency of the out put  $v_o$ , a and b component are noted.
4. For various frequency this steps are repeated.
5. The gain is  $20 \log v_o/v_{in}$  in db.

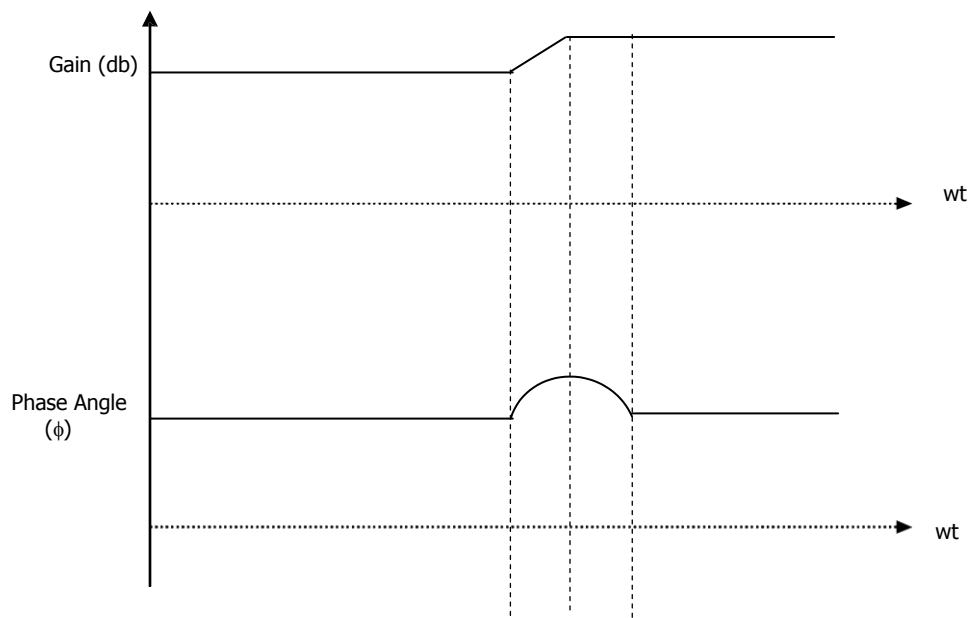
**Theory:-**

This consists in modifying the amplifier are the feed back network so as to add a zero to the transfer function there by increasing the phase. So that the magnitude of the gain remains unchanged and the phase margin gets increased.

This condition is achieved by placing a capacitor C in shunt connected with the resistor R. Now has an added positive phase shift in frequency range near the unity loop. Gain cross over point.

**Tabulation :-**

Sl.No.	Frequency	Output voltage (v)	Gain $A_v = 20 \log \frac{v_o}{v_{in}}$	Phase angle ( $\phi$ )

**Model Graph:-**

**Formula :-**

$$\theta = \tan^{-1}(WR_1C) - \tan^{-1}(WR_1 R_2C / R_1 + R_2)$$

$$\text{Gain : } A = 20 \log (v_o / v_{in}) \text{ db.}$$

$$\text{Transfer function: } \frac{1 + S R_2 C}{1 + SC (R_1 + R_2)}$$

**Design theory:-**

$$E_i(t) = (Z_1 + Z_2) i(t)$$

$$E_o(t) = Z_2(t)$$

$$Z_i(S) = \frac{R_1 \cdot 1/CS}{1 + R_1 S}$$

$$Z_2(S) = R_2$$

$$E_i(S) = (Z_1 + Z_2) I(S)$$

$$E_o(S) = Z_2 I(S)$$

$$\text{Put } S = J\omega$$

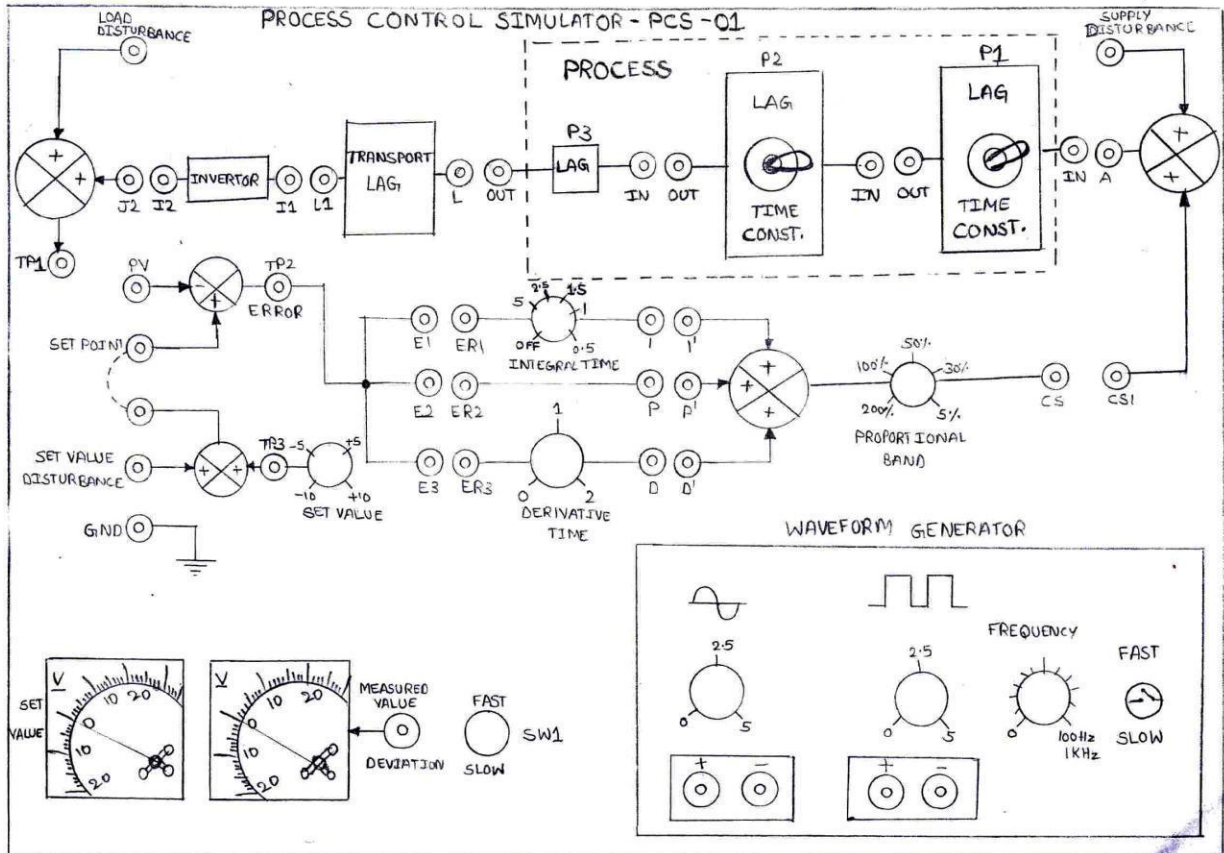
Transfer function:

$$T(S) = \frac{R_2 + J WR_1 R_2 C}{R_1 + R_2 + J WR_1 R_2 C}$$

**Result:-**

Thus the lead compensator was analyzed and transfer function of lead compensator was determined.

Study of PID Controller



**Exp. No:****Date:****STUDY OF PID CONTROLLER****Aim:-**

To determine the time constant and the time response of first order system.

**Apparatus required:-**

- 1.controller unit
- 2.CRS
- 3.Pitch cords

**Theory:-****Effect of proportional controller:-**

The proportional controller produces an o/p signal. Which is proportional to error signal. The transfer function of proportional is  $K_p$ . The term  $K_p$  is called the gain of controller. Hence the gain of the controller implies the error signal and increase the loop gain of the system behavior are improved by increased loop gain.

1. Steady state tracking accuracy
- 2 .Disturbance signal rejection
3. Relative stability

To increase in loop gain it decreases the sensitivity of the system. The drawback is proportional controller action is that it produces is constant steady state error.

**Effect of PI controller:-**

The proportional plus integral controller (PI) produces an o/p signal consisting of two term the one proportional to error signal and the other proportional to the integral of error signal.

$$\begin{aligned}\text{Tr.function of PI controller} &= K_p(1+1/T_i s) \\ &= K_p(T_i s+1/T_i s)\end{aligned}$$

Where  $K_p$  is equal to proportional gain and  $T_i$  is equal to integral time.

open loop Tr.function  $G(S) = \frac{\omega_n^2}{s(s+2\zeta\omega_n)}$  closed loop Tr. Function

$$\begin{aligned} c(s)/R(s) &= G(s)/1+G(S) \\ &= K_p \{ [1+T_i s/T_i] \omega_n^2 / s(s+\zeta\omega_n) \} / \{ 1+K_p [1+T_i s/T_i] \omega_n^2 / s(s+2\zeta\omega_n) \} \\ &= \{ (K_p/T_i) \omega_n^2 (1+T_i s) \} / \{ s^2 + 2\zeta\omega_n s + K_p \omega_n^2 + 2\zeta K_p T_i \omega_n^2 s \} \\ &= \{ (K_i \omega_n^2 (1+T_i s)) \} / \{ s^2 + 2\zeta\omega_n s + K_p \omega_n^2 \} \\ K_i &= K_p/T_i \end{aligned}$$

In the PI controller is used to reducing the steady state error and high order system less stable then lower order system.

### Effect of PD controller:-

The proportional plus derivatives controller produces an o/p signal consisting of two terms one proportional to error signal and other proportional to derivative of error signal.

The Tr.function of PD controller =  $K_p(1+T_d s)$

$K_p$  = proportional gain

$T_d$  = derivative time let the open loop Tr,function  $G(s)$  be second order system with

Tr.function  $G(s) = \frac{\omega_n^2}{s(s+2\zeta\omega_n)}$

$$\begin{aligned} C(S)/R(S) &= G(s)/1+G(s) = K_p(T_d s) \omega_n^2 / [1+K_p(1+T_d s)(\omega_n^2 / S(S+2\zeta\omega_n))] \\ &= \omega_n^2 (K_p + K_d s) / s^2 + (2\zeta\omega_n + K_d \omega_n^2) S + K_p \omega_n^2 \end{aligned}$$

where  $K_p = K_p T_d$ .

From the closed loop tr.function it is observed that the PD controller .Introduces a zero in the system and increases the damping Ratio Reduces the peak over shoot.

### PID CONTROLLER:-

A suitable combinational of the three basic modes,proportional Integral and derivative (PID) can improve an aspects of the system performance.

The proportional controller stabilize performance produces a steady state error. The integral controller reduces or eliminates the steady state error.The derivative controller reduces the rate of change of error. The combined effect of the three cannot be from the parameter  $K_p, K_i$  &  $K_d$ .

### PROCEDURE:-

- Make the ckt connection as per diagram.
- Calculate the peak amplitude of input square wave signal.
- Observe both input signal and output wave form on a cro.
- Then calculate the time taken by output signal to reach 65.2% of final value .

**P - CONTROLLER:-**

1. Make the connections as per fig.
2. Switch ON the power supply.
3. Square wave of amplitude 2Vpp is given as input with the optimum frequency setting and view the response on the CRO.
4. Adjust the proportional band knob.
5. From the response measure the peak over shoot from the setting value.
6. Note down the rise time, peak time, setting time for the given step input.
7. Repeat the above steps for various proportional bands.

**P-I CONTROLLER:-**

1. Make the connections as per fig.
2. Switch ON the power supply.
3. Square wave of amplitude 2Vpp is given as input with optimum frequency.
4. Adjust the value of the proportional and integral time knobs then view the response.
5. Repeat the above experiment for various proportional integral time and tabulate it .

**PID CONTROLLER:-**

1. Make the connections as per fig.
2. Switch ON the power supply .
3. Square wave of amplitude 2Vpp is given as input with the optimum frequency setting and view the response on the CRO.
4. Adjust the value of proportional band, integral time, and derivative knob and view the response on the CRO screen.
5. From the response measure the peak over shoot from the setting value.
6. Note down the rise time, peak time, setting time for the step input and note it .
7. Repeat the above steps for various proportional bands.

**RESULT:-**

Thus the time response of the first order system was determined.

**Ex.No:**

**Date:** **POLES AND ZEROS OF A TRANSFER FUNCTION**

**AIM:** To plot pole zero for a given transfer function in s-plane and z-plane using MATLAB

**LIST OF EQUIPMENT/SOFTWARE:**

Software : MATLAB

Category : soft experiment

**THERORY PART :**

**PROBLEM:**  $T(s) = Y(s)/R(s)$

$$= (8s^2+5s+1)/(s^2+2s+10)$$

Zero's  $\rightarrow (8s^2+5s+1)$  , the roots are  $s_1 = -0.3+j0.17$  &  $s_2 = -0.3-j0.17$

Pole's  $\rightarrow (s^2+2s+10)$  , the roots are  $s_3 = -1$  &  $s_4 = -1$



**PROGRAM PART :**

```
x=[8 5 1];
```

```
y=[1 2 1];
```

```
h=tf(x,y)
```

```
Pzmap(h)
```

**PROCEDURE :**

1. Open the MATLAB software
2. Open the command window
3. Enter the values and implements the commands
4. Save the program & run it
5. Verify the MATLAB output with theoretical output

**RESULT:**

Thus plotted the poles and zeros of a given transfer function using MATLAB

**Ex.No:**

**Date:**                    **BLOCK DIAGRAM REDUCTION TECHNIC**

**AIM:** The aim of the experiment is to learn MATLAB command that would be used to reduce linear system block diagram using series, parallel and feedback configuration

**LIST OF EQUIPMENT/SOFTWARE:**

Software        : MATLAB

Category        : soft experiment

**DELIVERABLES:** A complete lab report including the following

- Summarized learning outcomes
- MATLAB scripts and their result for experiments

**THEORETICAL PART :**

**Problem:**  $T_1(s) = 6/(s^2+3s+2)$  and  $T_2(s) = 9/(s+5)$  for the given transfer function find the output for blocks in series, parallel & eliminate the feed back

**PROGRAM PART:**

```
num1= [6];  
den1= [1 3 2];  
num2= [9];  
den2= [1 5];  
g1= tf(num1,den1)  
g2= tf(num2,den2)  
gs=series(g1,g2)  
gp=parallel(g1,g2)  
gf=feedback(g1,g2)
```

**PROCEDURE :**

1. Open the MATLAB software
2. Open the command window
3. Enter the values and implements the commands
4. Save the program & run it
5. Verify the MATLAB output with theoretical output

**RESULT:**

Thus the linear systems block diagram had been reduced theoretically and the same output was verified using MATLAB

**Ex.No:**

**Date:** **TIME DOMAIN ANALYSIS**

**AIM:** To compute and plot the unit step, ramp and impulse response using MATLAB

**LIST OF EQUIPMENT/SOFTWARE:**

Softwere : MATLAB

Category : soft experiment

**THEORETICAL PART :**

**PROBLEM:**  $Y(s)/R(s) = (2s+10)/(s^2+5s+4)$

**PROGRAM PART:****(i) Unit Step input**

```
num= [2 10];  
den= [1 5 4];  
g= tf(num,den)  
step(g)
```

**(ii) Impulse input**

```
num= [2 10];  
den= [1 5 4];  
g= tf(num,den)  
impulse(g)
```

**(iii) Ramp input**

```
num= [2 10];  
den= [1 5 4 0];  
g= tf(num,den)  
step(g)
```

**PROCEDURE :**

1. Open the MATLAB software
2. Open the command window
3. Enter the values and implements the commands
4. Save the program & run it
5. Verify the MATLAB output with theoretical output

**RESULT:**

Thus the time domain analysis was made for the given transfer function and also output was verified both theoretically & simulation

**Ex.No:**

**Date:**

## **FREQUENCY DOMAIN ANALYSIS**

**AIM:** In this experiment concept of bode plot and its phase margin & gain margin will be addressed using MATLAB

### **LIST OF EQUIPMENT/SOFTWARE:**

Software : MATLAB  
Category : soft experiment

### **THEORETICAL PART:**

**PROBLEM:** transfer function  $G(s) = 1250/s(s+5)(s+50)$  draw the bode plot obtain the frequency domain specification

**PROGRAM PART:**

```
num= [1250];  
den= [1 55 250 0];  
bode(num,den)  
grid  
title('bode plot for the transfer function  $G(s) = 1250/s(s+5)(s+50)$ )
```

**PROCEDURE :**

1. Open the MATLAB software
2. Open the command window
3. Enter the values and implements the commands
4. Save the program & run it
5. Verify the MATLAB output with theoretical output

**RESULT:**

Thus the concept of bode plot were studied using MATLAB

**Ex.No:**

**Date:**                    **STABILITY ANALYSIS USING ROOT LOCUS**

**AIM:** In this experiment concept of bode plot and its phase margin & gain margin will be addressed using MATLAB

**LIST OF EQUIPMENT/SOFTWARE:**

Software        : MATLAB

Category        : soft experiment

**THEORETICAL PART:**

**PROGRAM :**  $G(s) = k(s+0.2)/s^2(s+3.6)$



**PROGRAM PART :**

```
num= [1 0.2];  
den= [1 3.6 0 0];  
rlocus (num,den)  
axis(v)  
grid  
title('Root Locus for the transfer function  $G(s) = k(s+0.2)/s^2(s+3.6)$ ')
```

**PROCEDURE :**

1. Open the MATLAB software
2. Open the command window
3. Enter the values and implements the commands
4. Save the program & run it
5. Verify the MATLAB output with theoretical output

**RESULT:**

Thus the concept of root locus were studied using MATLAB